

Exercise 12

Calculate y' .

$$y = (\arcsin 2x)^2$$

Solution

Calculate y' by using the chain rule repeatedly.

$$\begin{aligned}y' &= \frac{d}{dx}(\arcsin 2x)^2 \\&= 2(\arcsin 2x)^1 \cdot \frac{d}{dx}(\arcsin 2x) \\&= 2(\arcsin 2x) \cdot \frac{1}{\sqrt{1 - (2x)^2}} \cdot \frac{d}{dx}(2x) \\&= 2(\arcsin 2x) \cdot \frac{1}{\sqrt{1 - 4x^2}} \cdot (2) \\&= \frac{4 \arcsin 2x}{\sqrt{1 - 4x^2}}\end{aligned}$$